

# CREATING GRAPHICS FROM SCRATCH

## CASE STUDIES

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# OUTLINE

## FIGURE 1: COMMUTATIVE DIAGRAM

The Figure and a Critique

Step 1: The Nodes

Step 2: The Edges

Step 3: Finishing Touches

## FIGURE 2: A PIE CHART

The Figure and a Critique

Detail 1: Elliptical Arcs

Detail 2: Perpendicular Lines

Detail 3: Shadings

## FIGURE 3: A CONSTRUCTION FROM EUCLID'S ELEMENTS

The Figure

Step 1: The Line  $AB$

Step 2: The Circles

Step 3: The Intersection of the Circles

Step 4: Finishing Touches

particular  $D$  is regular over  $M$ . Also  $\Delta \cap A = \Delta \cap \nu(A) = 1$ , so  $DE = D\hat{N} = \hat{N}E$ .

$$\begin{array}{ccccccc} \hat{N} & \xrightarrow{\quad} & \hat{N}(y) & \xrightarrow{\quad} & \hat{N}E' & \xrightarrow{\quad} & \hat{N}E \\ \downarrow & & \downarrow & & \downarrow & \nearrow D & \downarrow \\ M & \xrightarrow{\quad} & M(y) & \xrightarrow{\quad} & E' & \xrightarrow{\quad} & E \end{array}$$

Choose a Galois ring cover  $\hat{S}/R$  of  $\hat{N}E/M(y)$  [FJ05, Definition 6.1.3 and Remark 6.1.5] such that  $y \in R$  and  $x \in \hat{S}$ . Let  $U = \hat{S} \cap D$ . The ring extension  $U/R$  corresponds to a dominating separable rational map  $\text{Spec}(U) \rightarrow \text{Spec}(R)$ . Since the quotient field of  $R$  is a rational function field,  $\text{Spec}(R)$  is an open subvariety of an affine space. Therefore, by the definition of PAC extensions we have an  $M$ -epimorphism  $\varphi: U \rightarrow M$  with  $\alpha = \varphi(y) \in F$ . The field  $D$  is regular over  $M$  and  $D\hat{N} = \hat{N}E$ , hence  $\hat{S} = U \otimes_M \hat{N}$  [FJ05, Lemma 2.5.10]. Extend  $\varphi$  to an  $\hat{N}$ -epimorphism  $\varphi: \hat{S} \rightarrow \hat{N}$ . Then,  $\varphi$  induces a homomorphism  $\varphi^*: \text{Gal}(M) \rightarrow \text{Gal}(\hat{N}E/D)$  which satisfies  $\text{res}_{\hat{N}E, N} \circ \varphi^* = \text{res}_{M, \hat{N}}$ , where  $M_s$  is a separable closure of  $M$  [FJ05, Lemma 6.1.4]. Let  $\psi$  be the restriction of  $\varphi$  to  $\hat{S} = \hat{S} \cap E$ . The equality  $DE = \hat{N}E$  implies that  $\hat{S}$  is a subring of the quotient field of  $SU$ . Since  $\psi(\hat{S}) = \hat{N}$  and  $\psi(U) = M$  it follows that  $\psi(S) = \hat{N}$  and  $\psi^* = \text{res}_{\hat{N}E, E} \circ \varphi^*$ . From the commutative diagram

$$\begin{array}{ccc} & & \text{Gal}(M) \\ & \swarrow \psi^* & \downarrow \text{res} \\ \Delta & \xrightarrow{\quad} & \text{Gal}(\hat{N}/M) \\ & \nwarrow \psi^* & \downarrow \text{res} \\ & & \text{Gal}(E/E') \end{array}$$

it follows that  $(\psi^*)^{-1}(\nu(A_0)) = \text{res}_{M, \hat{N}}^{-1}(\text{Gal}(\hat{N}/N)) = \text{Gal}(N)$ . Consequently, the residue field of  $E'(x)$  under  $\psi$  is  $N$ . Also  $E' \subseteq D$  implies that the residue field of  $E'$  is  $M$ . Consequently,  $N = M(\beta)$ , where  $\beta = \psi(x)$  is a root of  $f(X, \alpha)$ . Finally, since  $[N : M] = n$ , the polynomial  $f(X, \alpha)$  is irreducible over  $M$ .

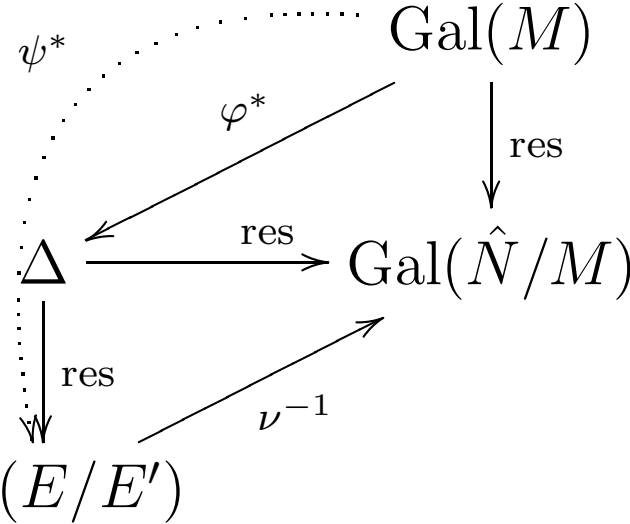
To complete the proof we need to find infinitely many  $\alpha \in F$  as above. This is done by the ‘Rabinovich trick’, that is, we replace  $R$  by the localization of  $R$  at  $\prod_{i=1}^n (y - \alpha_i)$  (see [JR94, Remark 1.2(c)]).  $\square$

**Corollary 2.** *Let  $M/F$  be a PAC extension, let  $f(X, y) \in M[X, y]$  be a polynomial of degree  $n$  in  $X$ , and let  $N/M$  be a separable extension of degree  $n$ . Assume that the Galois*

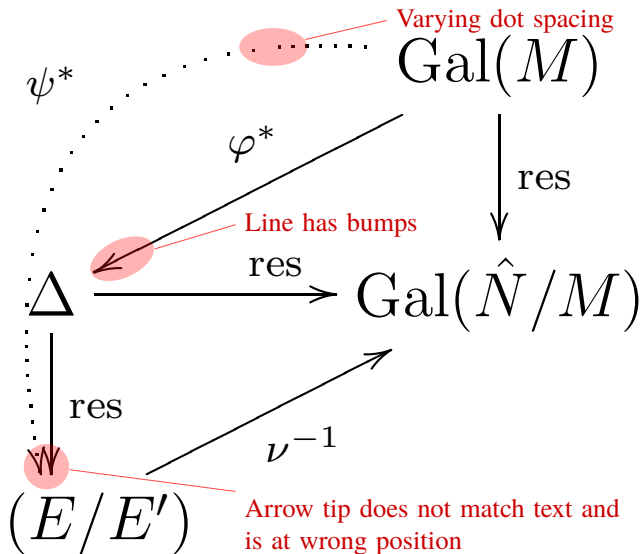


**Bary-Soroker Lior**  
 Dirichlet’s Theorem For  
 Polynomial Rings  
 arXiv:math/0612801v2

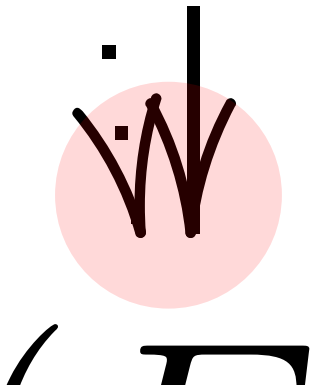
CLOSEUP OF THE FIGURE



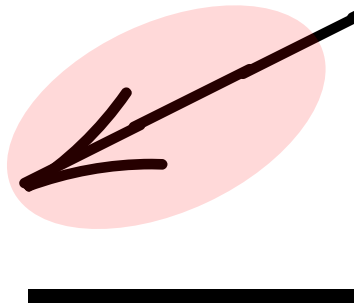
# CRITIQUE



## CLOSEUPS OF THE PROBLEMATIC AREAS.



Arrow tip does not match text and is at wrong position



Line has bumps

# STEP 1: CREATING THE NODES.

## BASIC IDEA

To (re)create the figure in TikZ, we start with the **nodes**, which are created using the `node` command.

## SYNTAX OF THE NODE CREATION COMMAND

- ▶ Start with `\node`.
- ▶ Then comes a sequences of **options**.
- ▶ Options are given in square brackets, with two exceptions:  
We can say `at` (coordinate) to specify a special place, where the node should go.  
We can say (name) to assign a name to a node.
- ▶ The node ends with some text in curly braces.

# STEP 1: CREATING THE NODES.

## A SIMPLE PLACEMENT

$\mathrm{Gal}(M)$

$\Delta$

$\mathrm{Gal}(\hat{N}/M)$

$(E/E')$

```
\begin{tikzpicture}
  \node (EE) at (0,0) {$(E/E')$};
  \node (Delta) at (0,1.5) {$\Delta$};
  \node (GalNM) at (3,1.5) {$\mathrm{Gal}(\hat{N}/M)$};
  \node (GalM) at (3,3) {$\mathrm{Gal}(M)$};
\end{tikzpicture}
```



# STEP 1: ALIGNING THE NODES

## BASIC IDEA.

### THE PROBLEM

Providing “hard-wired” coordinates like  $(3, 1.5)$  is **problematic**:

- ▶ When you read the code, it is hard to tell, where something will go.
- ▶ When you change something later, you may need to change many such coordinates.
- ▶ It is hard to make sure that all spacings and alignments are correct.

### POSSIBLE SOLUTIONS

- ▶ You can use options like `right=of Delta` to place a node relative to some other node.
- ▶ You can use a **TikZ-matrix**. It works like a  $\text{\LaTeX}$  matrix, only inside a picture.

# STEP 1: ALIGNING THE NODES.

ALIGNMENT USING A MATRIX.

$$\mathrm{Gal}(M)$$

$$\Delta$$

$$\mathrm{Gal}(\hat{N}/M)$$

$$(E/E')$$

```
\matrix[column sep=1cm,row sep=1cm]
{
    & \node (GalM)    {$\mathrm{Gal}(M)$}; & \\
    \node (Delta)    {$\Delta$}; & \node (GalNM)    {$\mathrm{Gal}(\hat{N}/M)$}; & \\
    \node (EE)       {$ (E/E') $}; & & \\
};
```

# STEP 1: ALIGNING THE NODES.

SIMPLIFIED VERSION...

$\mathrm{Gal}(M)$

$\Delta$

$\mathrm{Gal}(\hat{N}/M)$

$(E/E')$

```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes] (fig)
{
    & \mathrm{Gal} (M) & \\
    \Delta & \mathrm{Gal} (\hat{N}/M) & \\
    (E/E') & & \\
};
% Reference Gal(M) as (fig-1-2)
```

# STEP 1: ALIGNING THE NODES.

... WITH ALTERNATE NAMING OF NODES.

$$\mathrm{Gal}(M)$$

$$\Delta$$

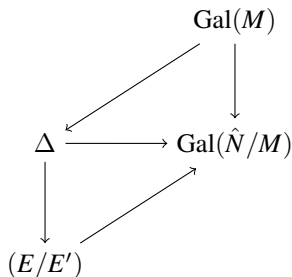
$$\mathrm{Gal}(\hat{N}/M)$$

$$(E/E')$$

```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes]
{
      & | (M) | & \mathrm{Gal} (M) & \\
| (Delta) | & \Delta & | (NM) | & \mathrm{Gal} (\hat{N}/M) & \\
| (EE) | & (E/E') & & & \\
};
% Reference Gal(M) as (M)
```

## STEP 2: CONNECTING THE NODES.

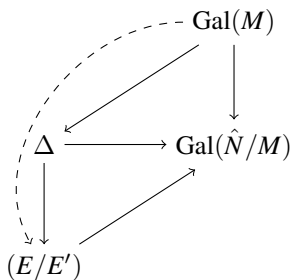
### SIMPLE STRAIGHT LINE.



```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes]
{
    & |(M)| & \Gal(M) & \\
    |(Delta)| & \Delta & |(NM)| & \Gal(\hat{N}/M) \\
    |(EE)| & (E/E') & & \\
};
\draw (M) edge [->] (Delta)
      (M) edge [->] (NM)
      (Delta) edge [->] (NM)
      (Delta) edge [->] (EE)
      (EE) edge [->] (NM);
```

## STEP 2: CONNECTING THE NODES.

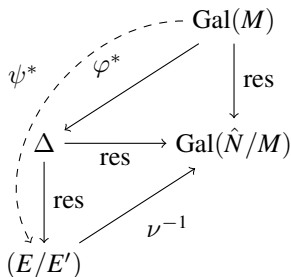
THE CURVED, DASHED LINE.



```
\draw (M)      edge [->] (Delta)
              edge [->] (NM)
              edge [->,dashed,out=180,in=120] (EE)
(Delta) edge [->] (NM)
        edge [->] (EE)
(EE)    edge [->] (NM);
```

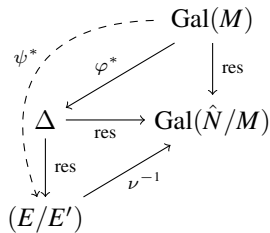
## STEP 2: CONNECTING THE NODES.

### ADDING THE LABELS



```
\draw [auto=right]
(M)      edge [->] node {\varphi^*} (Delta)
          edge [->] node [swap] {res} (NM)
          edge [->,dashed,out=180,in=120]
              node {\psi^*} (EE)
(Delta)  edge [->] node {res} (NM)
          edge [->] node [swap] {res} (EE)
(EE)     edge [->] node {\nu^{-1}} (NM);
```

### STEP 3: FINISHING TOUCHES



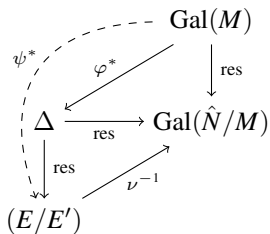
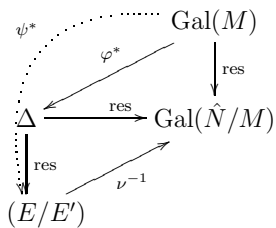
- ▶ Adjust “looseness” of the curve and dash phase.
- ▶ Reduce distance of  $\varphi^*$ ,  $\psi^*$  and  $\nu^{-1}$  to the line.
- ▶ Make edge labels smaller (as in  $A \xrightarrow{X} B$ )



# THE COMPLETE CODE.

```
\begin{tikzpicture}
  \matrix [column sep=7mm, row sep=7mm, matrix of math nodes]
  {
    & |(M)| & \Gal (M) & \\
    |(Delta)| & \Delta & |(NM)| & \Gal (\hat N/M) \\
    |(EE)| & (E/E') & & \\
  };
  \draw [auto=right, nodes={font=\scriptsize}]
    (M) edge [->] node [inner sep=0pt] {$\varphi^*$} (Delta)
        edge [->] node [swap] {res} (NM)
        edge [->, out=180, in=110, looseness=1.4,
              dashed, dash phase=3pt]
              node [inner sep=0pt] {$\psi^*$} (EE)
    (Delta) edge [->] node {res} (NM)
             edge [->] node [swap] {res} (EE)
    (EE) edge [->] node [inner sep=0pt] {$\nu^{-1}$} (NM);
\end{tikzpicture}
```

# COMPARISON OF ORIGINAL AND REWORKED FIGURE.

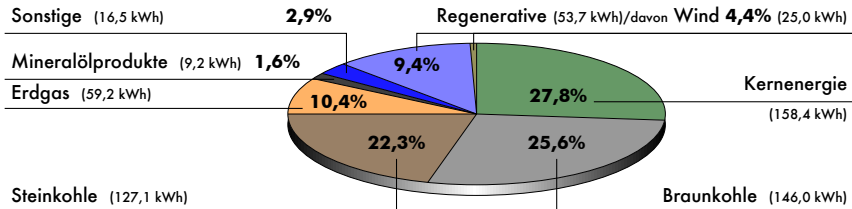


## A FIGURE FROM A MAJOR GERMAN NEWSPAPER.

### Kohle ist am wichtigsten

### Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)

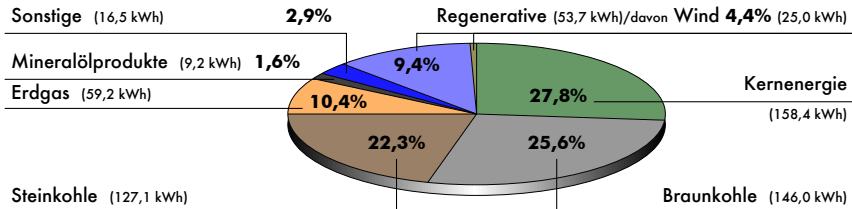


This figure is a redrawing of a figure from “Die Zeit,” June 4th, 2005.

## CRITIQUE.

### Kohle ist am wichtigsten Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



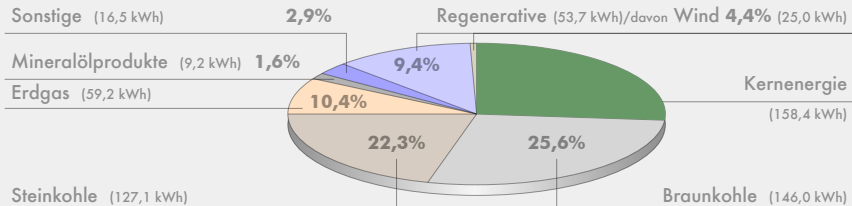
- ▶ Coloring is random and misleading.
- ▶ Pie slice sizes do not reflect percentages.
- ▶ Main message is lost since coal is split across page.

## DETAIL 1: PIE SLICES ARE ELLIPTIC ARCS.

### Kohle ist am wichtigsten

### Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



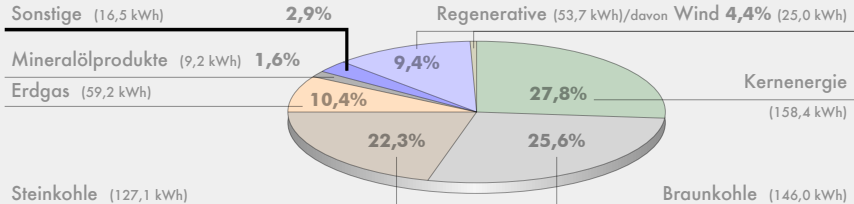
```
\fill[green!20!gray]
  (0,0)
  -- (90:1.2cm)
  arc[start angle=90, end angle=-5,
       x radius=3.2cm, y radius=1.2cm]
  -- cycle;
```

## DETAIL 2: A HORIZONTAL/VERTICAL JUNCTION.

### Kohle ist am wichtigsten

#### Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



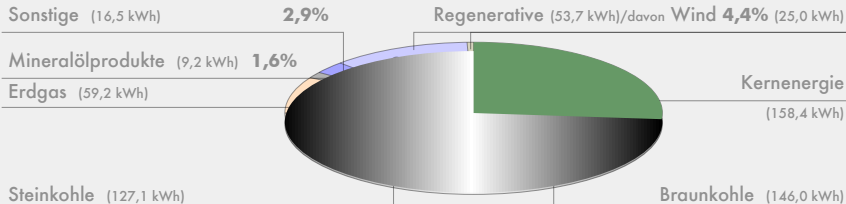
```
\draw[very thick] (-22mm,7mm) |- (-80mm,14mm);
```

## DETAIL 3: THE SHADING IN THE PIE CHART.

Kohle ist am wichtigsten

Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



```
\shade [left color=black,right color=black,middle color=white]
(0mm,-1.5mm) ellipse [x radius=3.2cm, y radius=1.2cm];

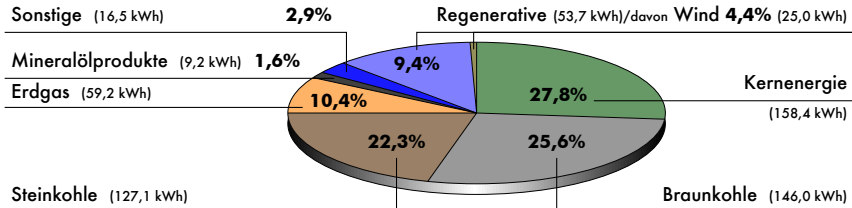
\fill[green!20!gray]
(0,0)
-- (90:1.2cm)
arc[start angle=90, end angle=-5,
x radius=3.2cm, y radius=1.2cm]
-- cycle;
```

# THE COMPLETE FIGURE.

## Kohle ist am wichtigsten

### Energiemix bei der deutschen Stromerzeugung 2004

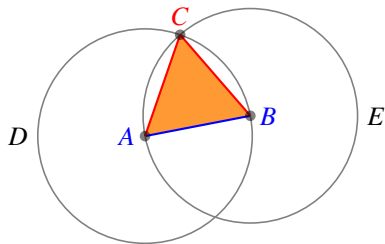
Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



The complete figure can be constructed in this way.



# A GEOMETRICAL CONSTRUCTION



Euclid of Alexandria  
Proof of Proposition I  
Elements, Book I

# STEP 1: THE LINE *AB*

## A SIMPLE LINE



```
\begin{tikzpicture}  
  \coordinate (A) at (0,0);  
  \coordinate (B) at (1.25,0.25);  
  
  \draw[blue] (A) -- (B);  
\end{tikzpicture}
```

- The `\coordinate` command is a shorthand for the `\node` command with empty text.

# STEP 1: THE LINE $AB$

## ADDING LABELS



```
\begin{tikzpicture}
  \coordinate [label=left:\textcolor{blue}{$A$}]
    (A) at (0,0);

  \coordinate [label=right:\textcolor{blue}{$B$}]
    (B) at (1.25,0.25);

  \draw[blue] (A) -- (B);
\end{tikzpicture}
```

- ▶ The `label` option makes it easy to add some text **around another node**.
- ▶ Alternatively, one could explicitly create a node later on.

# STEP 1: THE LINE $AB$

## PERTURBED POSITIONS



```
\usetikzlibrary{calc}
\begin{tikzpicture}
  \coordinate [label=left:\textcolor{blue}{$A$}]
    (A) at ($ (0,0) + .1*(rand,rand) $);

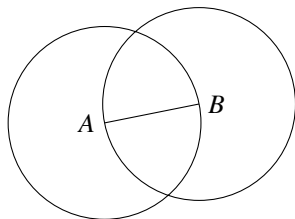
  \coordinate [label=right:\textcolor{blue}{$B$}]
    (B) at ($ (1.25,0.25) + .1*(rand,rand) $);

  \draw[blue] (A) -- (B);
\end{tikzpicture}
```

- Between  $(\$$  and  $\$)$  you can do some **basic linear algebra on coordinates**.

## STEP 2: THE CIRCLES

USING THE LET OPERATION



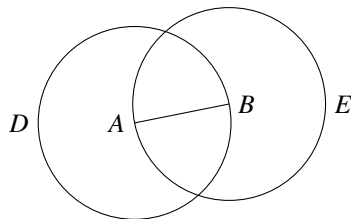
...

```
\draw (A) -- (B);
```

```
\draw let
    \p1          = ($ (B) - (A) $)
in
    (A) circle [radius={sqrt(\x1*\x1+\y1*\y1)}]
    (B) circle [radius={sqrt(\x1*\x1+\y1*\y1)}];
```

## STEP 2: THE CIRCLES

USING THE THROUGH LIBRARY



```
\usetikzlibrary{through}
```

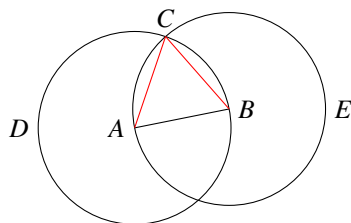
```
...
```

```
\draw (A) -- (B);
```

```
\node at (A) [draw,circle through=(B),label=left:$D$] {};
```

```
\node at (B) [draw,circle through=(A),label=right:$E$] {};
```

## STEP 3: THE INTERSECTION OF THE CIRCLES

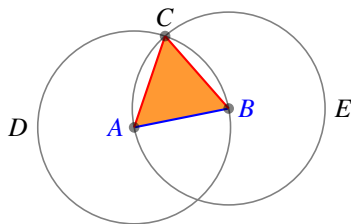


```
\usetikzlibrary{intersections}
...
\draw (A) -- (B);
\node at (A) [name path=D,draw,circle through=(B),label=...] {};
\node at (B) [name path=E,draw,circle through=(A),label=...] {};

\node [name intersections={of=D and E, by=C}]
  at (C) [above] {$C$};

\draw [red] (A) -- (C) (B) -- (C);
```

## STEP 4: FINISHING TOUCHES



- ▶ Add **transparent circles** at the points *A*, *B*, and *C*.
- ▶ Fill triangle, but on the **background layer**.



# THE COMPLETE CODE

```
\begin{tikzpicture} [thick,
                    help lines/.style={semithick,draw=black!50}]
\coordinate [label=left:\textcolor{blue}{$A$}]
  (A) at ($ (0,0) + .1*(rand,rand) $);
\coordinate [label=right:\textcolor{blue}{$B$}]
  (B) at ($ (1.25,0.25) + .1*(rand,rand) $);
\draw [blue] (A) -- (B);

\node at (A) [circle through=(B),name path=D,
             help lines,draw,label=left:$D$] {};
\node at (B) [circle through=(A),name path=E,
             help lines,draw,label=right:$E$] {};

\node [name intersections={of=D and E, by=C}]
  at (C) [above] {$C$};
\draw [red] (A) -- (C) (B) -- (C);

\foreach \point in {A,B,C}
  \fill [black,opacity=.5] (\point) circle (2pt);

\begin{pgfonlayer}{background}
  \fill[orange!80] (A) -- (C) -- (B) -- cycle;
\end{pgfonlayer}
\end{tikzpicture}
```